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Automatic Control with Interactive Tools

– Monograph –

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To Jimena, Julieta and Aurelia (J. L. Guzmán); to Marta and Belén (R. Costa); to Mari Paz, Laura and Ana (M. Berenguel); to María Antonia (S. Dormido)

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